

# Supplementary Information: Morpheme Ordering across Languages Reflects Optimization for Processing Efficiency

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## S1 Identifying Morphemes from Corpus Data

Here, we describe how we identified morphemes from corpus data and arrived at the classification of morphemes in the six languages as described in the main paper.

### S1.1 Korean Verb Suffixes

Korean verb morphology is very complex, and there is no generally agreed-upon description in terms of morphemes and slots. We extracted suffixes based on the annotation found in the corpus we used (Kaist corpus, Chun et al. [2018]) and the linguistic literature on Korean [Yeon and Brown, 2010]. The Kaist corpus already provides segmentation into morphemes; we postprocessed it in two ways: First, we made it more fine-grained by splitting morphemes that are merged in the annotation, and, second, we abstracted away consistently from allomorphy. For instance, the Kaist corpus separately labels the segments  $\text{ㄴ니다}$  *-mnida* (as in  $\text{합니다}$  *hamnida* ‘does’) and  $\text{습니다}$  *-seumnida* (as in  $\text{했습니다}$  *hatseumnida* ‘did’). These two segments actually are allomorphs, conditioned by the preceding material. Furthermore, they can both be segmented into the formal marker  $\text{ㅁ/습}$  (*-p/-seup*, we label this underlying morpheme “P<sub>5</sub>”, see below for

this notation), and the mood markers ㄴ (-ni, our NI<sub>6</sub>) and ㄷ (-da, our DA<sub>7</sub>). We therefore transform both segments into the abstract morpheme sequence P<sub>5</sub>-NI<sub>6</sub>-DA<sub>7</sub> (see below for this notation). We then partitioned the resulting morphemes into slots that make it possible to consistently describe the ordering of all forms encountered in the corpus. We indexed morphemes by a small-caps representation of a stylized phonological representation (such as P for -ㅍ/ㅍ -p/seup),<sup>1</sup> with a subscript indicating their slot (such as P<sub>5</sub>-NI<sub>6</sub>-DA<sub>7</sub>). With this procedure, we identified the slots described below:

1. Root
2. Derivation: The two derivational suffixes are *ha* ([Yeon and Brown, 2010, 4.1.2]) and the predicative *i*, whose function is similar to that of a copula [Yeon and Brown, 2010, 4.1.4].
3. Honorific SI<sub>3</sub> [Yeon and Brown, 2010, 4.3.2, 4.4.1]
4. Tense/Aspect suffixes include -ESS<sub>4</sub> for past [Yeon and Brown, 2010, 4.5.1.1], -ESSESS<sub>4</sub> for remote past [Yeon and Brown, 2010, 4.5.1.2], -GET<sub>4</sub> for future [Yeon and Brown, 2010, 4.5.2.1]
5. Formality P<sub>5</sub> (allomorphs include -p-, -m-, -seum-, [Yeon and Brown, 2010, 4.3.2])
6. Mood I: We partition Mood suffixes into two slots, as these can be combined into strings of combined mood suffixes. Frequent elements of the Mood I slot are -N<sub>6</sub>-, -NI<sub>6</sub>- [Yeon and Brown, 2010, 4.3.2].
7. Mood II: Frequent elements of the Mood II slot are declarative -DA<sub>7</sub>- [Yeon and Brown, 2010, 4.3.2], command -RA-, interrogative -KA-, the suffix -JI [Yeon and Brown, 2010, 4.2.2-3], and informal -EO<sub>7</sub>-.
8. Connective endings, such as -GE<sub>8</sub>, --SE<sub>8</sub>, and many others
9. Polite -YO<sub>9</sub>
10. Nominalizers, such as -GI<sub>10</sub> [Yeon and Brown, 2010, 2.2].

We show morphemes occurring at least 50 times in slots 2-8 in Figure S1. We do not provide the list of the (very numerous) conjunctive and nominalizing suffixes as these are not the focus of the typological generalization that we are interested in. Additional morphemes that do not fit into any of the slots and occur less than 50 times are placed into an UNKNOWN slot.

Next, we illustrate how our segmentation corresponds to commonly described paradigms. First, in Table S2, we describe the correspondence to the speech style system described by [Yeon and Brown, 2010, 4.3.2]. Second, in Tables S3–S5, we show an illustrative paradigm for the verb 하다 *hada* ‘to do’ as described in Wiktionary<sup>2</sup>, which covers some of the affixes in slots 4–7. In Table S6, we show the part of the paradigm of the verb *ida* ‘to be’ corresponding to Table S3 (the other parts of the paradigm are analogous to those of *hada*). Note that none of these paradigms constitute exhaustive lists of all forms of these verbs; instead, they represent commonly used forms in a systematic paradigmatic representation. We show these in order to illustrate how commonly used forms map onto morpheme sequences.

<sup>1</sup>These transcriptions are purely conventional, we do not intend these to correspond to a theory of how underlying phonological forms are realized as surface phone strings.

<sup>2</sup>Selection of forms and labeling of rows and columns in Tables S3–S6 are from <https://en.wiktionary.org/wiki/하다> and <https://en.wiktionary.org/wiki/있다> (retrieved September 16, 2020).

Slot	Morphs	Short	Description	Citation
Derivation	하	HA <sub>2</sub>		[Yeon and Brown, 2010, 4.1.2]
	이	I <sub>2</sub>		[Yeon and Brown, 2010, 4.1.4]
Honorific	시	SI <sub>3</sub>		[Yeon and Brown, 2010, 4.3.2, 4.4.1]
Tense/Asp.	였	ESSESS <sub>4</sub>		[Yeon and Brown, 2010, 4.5.1.2]
	겠	GET <sub>4</sub>	assertive	[Yeon and Brown, 2010, 4.5.2.1]
	쌌	ESS <sub>4</sub>	past	[Yeon and Brown, 2010, 4.5.1.1]
Formality	ㅅ	P <sub>5</sub>	formal-polite	[Yeon and Brown, 2010, 4.3.2]
Mood 1	리	RI <sub>6</sub>		
	니	NI <sub>6</sub>	See Table S3	[Yeon and Brown, 2010, 4.3.2]
	ㄴ	N <sub>6</sub>	See Table S3	
Mood 2	시	SIDA <sub>7</sub>	Hortative, formal, polite	
	어	EO <sub>7</sub>	Indicative, informal	
	자	JA <sub>7</sub>	Hortative	[Yeon and Brown, 2010, 4.3.6.3]
	소	SO <sub>7</sub>	See Table S2	
	ㄹ	LKKA <sub>7</sub>	Interrogative	[Yeon and Brown, 2010, 8.9]
	오	O <sub>7</sub>	See Table S2	
	지	JI <sub>7</sub>		[Yeon and Brown, 2010, 4.2.2-3]
	까	KA <sub>7</sub>	Interrogative	[Yeon and Brown, 2010, 4.3.4, p. 175; p. 183]
	라	RA <sub>7</sub>	command	[Yeon and Brown, 2010, 4.3.6.4]
다	DA <sub>7</sub>	Declarative	[Yeon and Brown, 2010, 4.3.2]	
Polite	요	YO <sub>9</sub>	See Table S2	

Table S1: Frequent Korean verb suffixes in slots 1-8. The first column describes the nine slots. Second column: Representation of one allomorph in Hangul. Third column: Identifier.

	Statement	Question	Command	Proposal
Formal	ㅁ니다 -mnida -P5-NI6-DA7	ㅁ니까 -mnikka -P5-NI6-KKA7	지-ㅁ-지오 -sipsio -SI3-P5-SIO7	지-ㅁ-지다 -sipsida -SI3-P5-SIDA7
Polite	아/어/요 -a/eoyo -EO7-YO9			
Semi-Formal	오/소 -o/so -O7/-SO7		오 -o -O7	-ㅁ-지다 -p-sida -P5-SIDA7
Familiar	네 -ne -NE7	나/는가 -na/neunka -NA7/-NEUNKA7	게 -ge -GE8	세 -se -SE8
Intimate	아/어 -a/eo -EO7			
Plain	다 -da -DA7	(느)냐 -(neu)nya -NYA7	라 -ra -RA7	자 -ja -JA7

Table S2: Correspondence between our morpheme segmentation and the speech style system described by [Yeon and Brown, 2010, 4.3.2]. In each cell, we provide the Hangeul ending given by [Yeon and Brown, 2010], a transliteration, and a representation in terms of underlying morphemes.

		Formal non-polite	Informal non-polite	Informal polite	Formal polite
Indicative	Non-past	한다	해	해요	합니다
		handa	hae	haeyo	hamnida
		-N <sub>6</sub> -DA <sub>7</sub>	-EO <sub>7</sub>	-EO <sub>7</sub> -YO <sub>9</sub>	-P <sub>5</sub> -NI <sub>6</sub> -DA <sub>7</sub>
		하+ㄴ 다 px+ef	하+어 pvg+ecs	하+어+요 pvg+ef+jxf	하+ㅁ 니다 pvg+ef
Past	Past	했다	했어	했어요	했습니다
		haet-da	haesseo	haesseoyo	haetseumnida
		-ESS <sub>4</sub> -DA <sub>7</sub>	-ESS <sub>4</sub> -EO <sub>7</sub>	-ESS <sub>4</sub> -EO <sub>7</sub> -YO <sub>9</sub>	-ESS <sub>4</sub> -P <sub>5</sub> -NI <sub>6</sub> -DA <sub>7</sub>
		하+였+다 ncpa+xsv+ep+ef	하+였+어 px+ep+ef	하+였+어+요 px+ep+ef+jxf	하+였+습니다 pvg+ep+ef
Interrogative	Non-past	하느냐	해	해요	합니까
		haneunya	hae	haeyo	hamnikka
		-NYA <sub>7</sub>	-EO <sub>7</sub>	-EO <sub>7</sub> -YO <sub>9</sub>	-P <sub>5</sub> -NI <sub>6</sub> +KKA <sub>7</sub>
		하+느냐 px+ef			하+ㅁ 니까 px+ef
Hortative	Past	했느냐	했어	했어요	했습니다까
		ha-n-neunya	hae-sseo	hae-sseo-yo	haetseumnikka
		-ESS <sub>4</sub> -NYA <sub>7</sub>	-ESS <sub>4</sub> -EO <sub>7</sub>	-ESS <sub>4</sub> -EO <sub>7</sub> -YO <sub>9</sub>	-ESS <sub>4</sub> -P <sub>5</sub> -NI <sub>6</sub> -KKA <sub>7</sub>
		하+였+느냐 +ep+ef	하+였+어 +ep+ef	하+였+어+요 px+ep+ef+jxf	하+였+습니까 pvg+ep+ef
Imperative	Hortative	하자	해	해요	합시다
		haja	hae	haeyo	hapsida
		-JA <sub>7</sub>	-EO <sub>7</sub>	-EO <sub>7</sub> -YO <sub>9</sub>	-P <sub>5</sub> -SIDA <sub>7</sub>
		+자 +ef		하+어+요 pvg+ef+jxf	하+ㅁ 시다 ef
Assertive	Imperative	해라, 하여라	해	해요	합시오
		haera, hayeora	hae	haeyo	hapsio
		-RA <sub>7</sub>	-EO <sub>7</sub>	-EO <sub>7</sub> -YO <sub>9</sub>	-P <sub>5</sub> -SI <sub>3</sub> O
		하+어라, 하+어라 pvg+ef, pvg+ef			+ㅁ 시오 +ef
Assertive	Assertive	하겠다	하겠어	하겠어요	하겠습니다
		hagetda	hagesseo	hagesseoyo	hagetseumnida
		-GET <sub>4</sub> -DA <sub>7</sub>	-GET <sub>4</sub> -EO <sub>7</sub>	-GET <sub>4</sub> -EO <sub>7</sub> -YO <sub>9</sub>	GET <sub>4</sub> -P <sub>5</sub> -NI <sub>6</sub> -DA <sub>7</sub>
		하+겠+다 px+ep+ef	하+겠+어 pvg+ep+ef	하+겠+어+요 pvg+ep+ef+jxf	하+겠+습니다 pvg+ep+ef

Table S3: Selected forms of *hada* ‘to do’ (see text for further information). In each cell, we provide Hangul and transliterated (e.g., handa) forms, a representation in terms of underlying morphemes (e.g., -N<sub>6</sub>-DA<sub>7</sub>), and – where available – how the form is segmented in the Kaist corpus (e.g., px+ef).

	Formal non-polite	Informal non-polite	Informal polite	Formal polite
Cause/Reason	해 hae -EO7	해서, 하여서 haeseo, hayeoseo -EOSEO8 하+어서, 하+어서 pvg+ecs, xsm+ecs	하니 hani -NI8 하+니 pvg+ecs	하니까 hanikka -NIKKA8 하+니까 xsm+ef
Contrast	하지만 hajiman -JIMAN8	하는데 haneunde -NEUNDE8	하더니 haedoni -DEONI8	
Conjunction	하고 hago -GO8			
Condition	하면 hamyeon -MYEON8	해야, 하여야 haeya, hayeoya -EOYA8		
Motive	하려고 haryeogo -RYEOGO8			

Table S4: Continuation of Table S3: Forms of *hada* with a conjunctive ending.

		Formal non-polite	Informal non-polite	Informal polite	Formal polite
Indicative	Non-past	하신다 -SI3-N6-DA7 하+시+ㄴ다	하셔 SI3-EO7 -	하세요, 하세요 SI3-EO7-YO 하+시+어+요	하십니다 SI3-P5-NI6-DA7 하+시+ㅁ니다
		하셨다 SI3-ESS4-DA7 하+셨+다	하셨어 SI3-ESS4-EO7 -	하셨어요 SI3-ESS4-EO7-YO -	하셨습니다 SI3-ESS4-P5-NI6-DA7 하+셨+습니다
Interrogative	Non-past	하시느냐 SI3-NYA7 -	하셔 SI3-EO7 -	하세요, 하세요 SI3-EO7-YO 하+시+어+요	하십니까 SI3-P5-NI6-KKA7 -
		Past	하셨느냐 SI3-ESS4-NYA7	하셨어 SI3-ESS4-EO7	하셨어요 SI3-ESS4-EO7-YO
Imperative		하시라 -SI3-RA	하셔 -SI3-EO7 하+시+어+	하세요 -SI3-EO7-YO 하+십시오	하십시오 -SI3-P5-SI3O
Assertive		하시겠다 -SI3-GET4-DA7 -	하시겠어 -SI3-GET4-EO7 -	하시겠어요 -SI3-GET4-EO7-YO -	하시겠습니다 -SI3-GET4-P5-NI6-DA7 -

Table S5: Continuation of Tables S3–S4: Selected forms of *hada* with an honorific (SI3). We provide Hangul forms, morpheme sequences, and – where available – segmentations as given in the Kaist corpus.

		Formal non-polite	Informal non-polite	Informal polite	Formal polite
Indicative	Non-past	있다	있어	있어요	있습니다
		있+다	있+어	있+어+요	있+습니다
	Past	-DA <sub>7</sub>	-EO <sub>7</sub>	-EO <sub>7</sub> -YO	-P <sub>5</sub> -NI <sub>6</sub> -DA <sub>7</sub>
		+ef	+ef	+ef+jxf	+ef
Interrogative	Non-past	있느냐	있어	있어요	있습니까
		있+느냐	있+어	있+어+요	있+습니까
	Past	-NYA <sub>7</sub>	-EO <sub>7</sub>	-EO <sub>7</sub> -YO	-P <sub>5</sub> -NI <sub>6</sub> -KKA <sub>7</sub>
		+ef	+ef	+ef+jxf	+ef
Assertive	Non-past	있겠냐	있겠어	있겠어요	있겠습니까
		있+겠냐	있+겠어	있+겠어+요	있+겠습니까
	Past	-GET <sub>4</sub> -DA <sub>7</sub>	-GET <sub>4</sub> -EO <sub>7</sub>	-GET <sub>4</sub> -EO <sub>7</sub> -YO	-GET <sub>4</sub> -P <sub>5</sub> -NI <sub>6</sub> -DA <sub>7</sub>
		+ep+f	+ep+ef	paa+ep+ef+jxf	paa+ep+ef

Table S6: Selected forms of *itda*. Refer to Table S3 for details.

## S1.2 Finnish Verb Inflection

In the Finnish corpus, verb forms are annotated using collections of features, such as Mood=Ind and Number=Sing, which make it possible to uniquely map the form to a cell of the paradigm in Table S7.<sup>3</sup> Additionally, Finnish verbs can take various final clitics [Karlsson, 1999, Section 91].

## S1.3 Turkish Verb Suffixes

In Table S8, we show the list of identified Turkish verb suffixes [van Schaaik, 2020].<sup>4</sup> In Figure S9, we illustrate this using selected forms of *yapmak*, covering TAM and agreement suffixes.<sup>5</sup>

## S1.4 Hungarian Verb Suffixes

In Table S10, we show the list of identified Hungarian verb suffixes [Rounds, 2001]. In Figure S11, we illustrate these using selected forms of three verbs.<sup>6</sup>

<sup>3</sup>For illustration, we provide forms of *tulla* from <https://en.wiktionary.org/wiki/tulla#Conjugation>, retrieved January 10, 2021.

<sup>4</sup>Note that there are some further derivational forms, such as reciprocal *-(I)ş* as in *görüş-* ‘to meet’ derived from *gör-* ‘to see’. However, these are not annotated in the Universal Dependencies data, which treats the derived form as the lemma.

<sup>5</sup>The selection of forms follows: <https://en.wiktionary.org/wiki/yapmak#Turkish>, retrieved September 5, 2020.

<sup>6</sup>The selection of forms follows <https://en.wiktionary.org/wiki/tesz>, <https://en.wiktionary.org/wiki/csinál>, <https://en.wiktionary.org/wiki/ismer>, retrieved September 5, 2020.

TAM	Agreement	Form	Suffixes
present tense [Karlsson, 1999, Section 24]	1st sing.	tulen	-n <sub>AGR</sub>
	2nd sing.	tulet	-t <sub>AGR</sub>
	3rd sing.	tulee	-V <sub>AGR</sub>
	1st plur.	tulemme	-mme <sub>AGR</sub>
	2nd plur.	tulette	-tte <sub>AGR</sub>
	3rd plur.	tulevat	-vat <sub>AGR</sub>
	passive	tullaan	-t <sub>PASSIVE</sub> -Vn <sub>AGR</sub>
past tense [Karlsson, 1999, Section 60]	1st sing.	tulin	-i <sub>TAM</sub> -n <sub>AGR</sub>
	2nd sing.	tulit	-i <sub>TAM</sub> -t <sub>AGR</sub>
	3rd sing.	tuli	-i <sub>TAM</sub> -V <sub>AGR</sub>
	1st plur.	tulimme	-i <sub>TAM</sub> -mme <sub>AGR</sub>
	2nd plur.	tulitte	-i <sub>TAM</sub> -tte <sub>AGR</sub>
	3rd plur.	tulivat	-i <sub>TAM</sub> -vat <sub>AGR</sub>
	passive	tultiin	-t <sub>PASSIVE</sub> -i <sub>TAM</sub> -Vn <sub>AGR</sub>
conditional mood (-isi-, [Karlsson, 1999, Section 65])	1st sing.	tulisin	-isi <sub>TAM</sub> -n <sub>AGR</sub>
	2nd sing.	tulisit	-isi <sub>TAM</sub> -t <sub>AGR</sub>
	3rd sing.	tulisi	-isi <sub>TAM</sub> -V <sub>AGR</sub>
	1st plur.	tulisimme	-isi <sub>TAM</sub> -mme <sub>AGR</sub>
	2nd plur.	tulisitte	-isi <sub>TAM</sub> -tte <sub>AGR</sub>
	3rd plur.	tulisivat	-isi <sub>TAM</sub> -vat <sub>AGR</sub>
	passive	tultaisiin	-ta <sub>PASSIVE</sub> -isi <sub>TAM</sub> -Vn <sub>AGR</sub>
imperative mood [Karlsson, 1999, Section 66]	1st sing.	–	
	2nd sing.	tule	-
	3rd sing.	tulkoon	-kV <sub>TAM</sub> -oon <sub>AGR</sub>
	1st plur.	tulkaamme	-kV <sub>TAM</sub> -mme <sub>AGR</sub>
	2nd plur.	tulkaa	-kV <sub>TAM</sub>
	3rd plur.	tulkoot	-kV <sub>TAM</sub> -vat <sub>AGR</sub>
	passive	tultakoon	-ta <sub>PASSIVE</sub> -kV <sub>TAM</sub> -Vn <sub>AGR</sub>
potential mood (-ne-, [Karlsson, 1999, Section 67])	1st sing.	tullen	-ne <sub>TAM</sub> -n <sub>AGR</sub>
	2nd sing.	tullet	-ne <sub>TAM</sub> -t <sub>AGR</sub>
	3rd sing.	tullee	-ne <sub>TAM</sub> -V <sub>AGR</sub>
	1st plur.	tullemme	-ne <sub>TAM</sub> -mme <sub>AGR</sub>
	2nd plur.	tullette	-ne <sub>TAM</sub> -tte <sub>AGR</sub>
	3rd plur.	tullevat	-ne <sub>TAM</sub> -vat <sub>AGR</sub>
	passive	tultaneen	-t <sub>PASSIVE</sub> -ne <sub>TAM</sub> -Vn <sub>AGR</sub>

Table S7: Selected forms of Finnish verbs. See text for details.



Slot	Label	Function	Morphs	Reference
Valence	TIR <sub>1</sub>	Causative	-tIr	
Voice	IL <sub>2</sub>	Passive	-Il	
Polarity	MA <sub>3</sub>	Negation	-mA	
Mood	EBIL <sub>4</sub>	Abilitative	-Ebil	van Schaaik [2020], section 21
	IN <sub>4</sub>	Imperative	-In	van Schaaik [2020], section 18.1
TAM1	AR <sub>5</sub>	Aorist	-(I/E)r, -z	van Schaaik [2020], section 20.5 ('Present-2')
	IYOR <sub>5</sub>	Imperfective	-Iyor	
	ACAK <sub>5</sub>	Future	-AcAk	van Schaaik [2020], section 20.2
	MIS <sub>5</sub>	Perfective	-mİş	van Schaaik [2020], section 20.3
	TI <sub>5</sub>	Past	-dİ	van Schaaik [2020], section 20.4
3rd Plural	lar <sub>6</sub>	3rd Plural	-lAr	
TAM2	MUS <sub>27</sub>	Aorist	-mİş	van Schaaik [2020], section 24.2
	DU <sub>7</sub>	Past	-dİ	van Schaaik [2020], section 24.1.3
Agreement	IM <sub>8</sub>	1st singular	-Im	
	SIN <sub>8</sub>	2nd singular	-sIn	
	IZ <sub>8</sub>	1st plural	-Iz	
	SINIZ <sub>8</sub>	2nd plural	-sInIz	
	K <sub>8</sub>	1st plural, past direct	-k	

Table S8: Verb suffixes in Turkish, arranged by slot. The first column describes slots as in the main paper. The second column lists the unique identifiers for each morpheme. The third column describes the function and meaning; the fourth column describes the approximate phonological form (see van Schaaik [2020, Section 5.1] for the vowels I, A, E).

		1 sg.	2 sg.	3 sg.	1 pl.	2 pl.	3 pl.
Indicative Non-Past	Aorist	yaparım -AR <sub>5</sub> -IM <sub>8</sub>	yaparsın -AR <sub>5</sub> -SIN <sub>8</sub>	yapar -AR <sub>5</sub>	yaparız -AR <sub>5</sub> -IZ <sub>8</sub>	yaparsınız -AR <sub>5</sub> -SINIZ <sub>8</sub>	yaparlar -AR <sub>5</sub> -LAR <sub>6</sub>
	Imperfective	yapıyorum -IYOR <sub>5</sub> -IM <sub>8</sub>	yapıyorsun -IYOR <sub>5</sub> -SIN <sub>8</sub>	yapıyor -IYOR <sub>5</sub>	yapıyoruz -IYOR <sub>5</sub> -IZ <sub>8</sub>	yapıyorsunuz -IYOR <sub>5</sub> -SINIZ <sub>8</sub>	yapıyorlar -IYOR <sub>5</sub> -LAR <sub>6</sub>
	Future	yapacağım -ACAK <sub>5</sub> -IM <sub>8</sub>	yapacaksın -ACAK <sub>5</sub> -SIN <sub>8</sub>	yapacak -ACAK <sub>5</sub>	yapacağız -ACAK <sub>5</sub> -IZ <sub>8</sub>	yapacaksınız -ACAK <sub>5</sub> -SINIZ <sub>8</sub>	yapacaklar -ACAK <sub>5</sub> -LAR <sub>6</sub>
Indicative Past	Perfective	yaptım -TI <sub>5</sub> -IM <sub>8</sub>	yaptın -TI <sub>5</sub> -SIN <sub>8</sub>	yaptı -TI <sub>5</sub>	yaptık -TI <sub>5</sub> -K <sub>8</sub>	yaptınız -TI <sub>5</sub> -SINIZ <sub>8</sub>	yaptılar -TI <sub>5</sub> -LAR <sub>6</sub>
	Imperfective	yapıyordum -IYOR <sub>5</sub> -DU <sub>7</sub> -IM <sub>8</sub>	yapıyordun -IYOR <sub>5</sub> -DU <sub>7</sub> -SIN <sub>8</sub>	yapıyordu -IYOR <sub>5</sub> -DU <sub>7</sub>	yapıyorduk -IYOR <sub>5</sub> -DU <sub>7</sub> -K <sub>8</sub>	yapıyordunuz -IYOR <sub>5</sub> -DU <sub>7</sub> -SINIZ <sub>8</sub>	yapıyorlardı -IYOR <sub>5</sub> -LAR <sub>6</sub> -DU <sub>7</sub>
Non-Indicative	Perfective	yapmışım -MIS <sub>5</sub> -IM <sub>8</sub>	yapmışsın -MIS <sub>5</sub> -SIN <sub>8</sub>	yapmış -MIS <sub>5</sub>	yapmışız -MIS <sub>5</sub> -IZ <sub>8</sub>	yapmışsınız -MIS <sub>5</sub> -SINIZ <sub>8</sub>	yapmışlar -MIS <sub>5</sub> -LAR <sub>6</sub>
	Aorist	yaparmışım -AR <sub>5</sub> -MIS <sub>7</sub> -IM <sub>8</sub>	yaparmışsın -AR <sub>5</sub> -MIS <sub>7</sub> -SIN <sub>8</sub>	yaparmış -AR <sub>5</sub> -MIS <sub>7</sub>	yaparmışız -AR <sub>5</sub> -MIS <sub>7</sub> -IZ <sub>8</sub>	yaparmışsınız -AR <sub>5</sub> -MIS <sub>7</sub> -SINIZ <sub>8</sub>	yaparlarmış -AR <sub>5</sub> -LAR <sub>6</sub> -MIS <sub>7</sub>
	Imperfective	yapıyormuşum -IYOR <sub>5</sub> -MIS <sub>7</sub> -IM <sub>8</sub>	yapıyormuşsun -IYOR <sub>5</sub> -MIS <sub>7</sub> -SIN <sub>8</sub>	yapıyormuş -IYOR <sub>5</sub> -MIS <sub>7</sub>	yapıyormuşuz -IYOR <sub>5</sub> -MIS <sub>7</sub> -IZ <sub>8</sub>	yapıyormuşsunuz -IYOR <sub>5</sub> -MIS <sub>7</sub> -SUNUZ <sub>8</sub>	yapıyorlarmış -IYOR <sub>5</sub> -LAR <sub>6</sub> -MIS <sub>7</sub>

Table S9: Illustrating Turkish verb suffixes using selected forms of the verb *yapmak*, covering TAM and agreement suffixes (slots 5–8). Note that the labeling of TAM categories varies between grammars, and our choices here are only intended to provide a broad orientation. See text for details.

Slot	Morpheme	Function	Reference
Valence	AT <sub>VAL</sub>	Causative	Rounds [2001] 4.5.3
Mood	HET <sub>MOOD</sub>	Potential	Rounds [2001] 4.5.1
	NE <sub>MOOD</sub>	conditional	Rounds [2001] 4.3.7
	J <sub>MOOD</sub>	subjunctive	Rounds [2001] 4.3.5
Tense	T <sub>TENSE</sub>	indicative past	Rounds [2001] 4.3.3
Agreement (Obj+Subj)		See Table S11	Rounds [2001] 4.3

Table S10: Hungarian verb suffixes

In addition to finite verbs, infinitives are also labeled as verbs in the corpus. These have an ending *-ni* [Rounds, 2001, 4.4.4]; we assign it a slot “Nominal” for our analysis..

### S1.5 Sesotho

We describe Sesotho verb affixes following Hahn et al. [2021]. who described these based on [Doke and Mofokeng, 1967, Guma, 1971, Demuth, 1992]. We refer to Hahn et al. [2021] for further details.

1. Subject agreement: This morpheme encodes agreement with the subject, for person, number, and noun class (the latter only in the 3rd person) [Doke and Mofokeng, 1967, §395]. The annotation provided by Demuth [1992] distinguishes between ordinary subject agreement prefixes and agreement prefixes used in relative clauses; we distinguish these morpheme types here.
2. Negation [Doke and Mofokeng, 1967, §429]
3. Tense/aspect marker [Doke and Mofokeng, 1967, §400–424]
4. Object agreement or reflexive marker [Doke and Mofokeng, 1967, §459]. Similar to subject agreement, object agreement denotes person, number, and noun class features of the object.

We identified the following suffixes:

1. Semantic derivation: reversive (e.g., ‘do’ → ‘undo’)
2. Valence: (e.g., causative, neuter/stative, applicative, and reciprocal)
3. Voice: passive
4. Tense/Aspect
5. Mood
6. Relative marker, marking verbs in relative clauses

### S1.6 Japanese

We describe Japanese verb suffixes following [Hahn et al., 2021], who described these based on [Kaiser et al., 2013, Hasegawa, 2014]. We refer to [Hahn et al., 2021] for details.

		Singular			Plural			Rounds [2001]
		1	2	3	1	2	3	
Ind	Pres I	teszek csinálok ismerek -ek -EK <sub>AGR</sub>	teszel csinálsz ismersz -sz -EL <sub>AGR</sub>	tesz csinál ismer - -	teszünk csináunk ismerünk -ünk -UNK <sub>AGR</sub>	tesztek csináltak ismertek -tek -TEK <sub>AGR</sub>	tesznek csinálnak ismernek -nek -NEK <sub>AGR</sub>	4.3.1.1
	D	teszem csinádom ismerem -em -EM <sub>AGR</sub>	teszed csináod ismered -ed -ED <sub>AGR</sub>	teszi csinálja ismeri -i -I <sub>AGR</sub>	tesszük csináljuk ismerjük -jük -IUK <sub>AGR</sub>	teszitek csináljátok ismertek -itek -ITEK <sub>AGR</sub>	teszik csinálják ismerik -ik -IK <sub>AGR</sub>	4.3.1.2
Past	I	tettem csináltam ismertem -t-em -T <sub>TENSE</sub> -EM <sub>AGR</sub>	tettél csináltál ismertél -t-él -T <sub>TENSE</sub> -EEL <sub>AGR</sub>	tett csinált ismert -t -T <sub>AGR</sub>	tettünk csináltunk ismertünk -t-ünk -T <sub>TENSE</sub> -UNK <sub>AGR</sub>	tettetek csináltatok ismertetek -t-etek -T <sub>TENSE</sub> -ETEK <sub>AGR</sub>	tették csináltak ismertek -t-ek -T <sub>TENSE</sub> -EK <sub>AGR</sub>	4.3.3.1
	D	tettem csináltam ismertem -t-em -T <sub>TENSE</sub> -EM <sub>AGR</sub>	tetted csináltad ismerted -t-ed -T <sub>TENSE</sub> -ED <sub>AGR</sub>	tette csinálta ismerte -t-e -T <sub>TENSE</sub> -I <sub>AGR</sub>	tettük csináltuk ismertük -t-ük -T <sub>TENSE</sub> -UK <sub>AGR</sub>	tettétek csináltátok ismertétek -t-étek -T <sub>TENSE</sub> -EETEK <sub>AGR</sub>	tették csinálták ismerték -t-ék -T <sub>TENSE</sub> -EEK <sub>AGR</sub>	4.3.3.2
Cond	Pres I	tennék csinálnék ismernék -nék -NE <sub>MOOD</sub> -EK <sub>AGR</sub>	tennél csinálnál ismernél -nél -NE <sub>MOOD</sub> -EL <sub>AGR</sub>	tenne csinálna ismerne -ne -NE <sub>MOOD</sub>	tennénk csinálnánk ismernénk -nénk -NE <sub>MOOD</sub> -ENK <sub>AGR</sub>	tennétek csinálnátok ismernétek -nétek -NE <sub>MOOD</sub> -ETEK <sub>AGR</sub>	tennének csinálnának ismernének -nének -NE <sub>MOOD</sub> -ENEK <sub>AGR</sub>	4.3.7.1
	D	tenném csinálnám ismerném -ném -NE <sub>MOOD</sub> -EM <sub>AGR</sub>	tennéd csinálnád ismernéd -néd -NE <sub>MOOD</sub> -ED <sub>AGR</sub>	tenné csinálná ismerné -né -NE <sub>MOOD</sub> -E <sub>AGR</sub>	tennénk csinálnánk ismernénk -nénk -NE <sub>MOOD</sub> -ENK <sub>AGR</sub>	tennétek csinálnátok ismernétek -nétek -NE <sub>MOOD</sub> -ETEK <sub>AGR</sub>	tennének csinálnának ismernék -nék -NE <sub>MOOD</sub> -EK <sub>AGR</sub>	4.3.7.2
Subj	Pres I	tegyek csináljak ismerjek -j-ek -J <sub>MOOD</sub> -EK <sub>AGR</sub>	tégy or tegyél csinálj or csináljál ismerj or ismerjél -j-(él) J <sub>MOOD</sub> -EEL <sub>AGR</sub>	tegyen csináljon ismerjen -j-en -J <sub>MOOD</sub> -EN <sub>AGR</sub>	tegyünk csináljunk ismerjünk -j-ünk -J <sub>MOOD</sub> -UNK <sub>AGR</sub>	tegyetek csináljátok ismerjétek -j-etek -J <sub>MOOD</sub> -ETEK <sub>AGR</sub>	tegyenek csináljanak ismerjenek -j-enek -J <sub>MOOD</sub> -ENEK <sub>AGR</sub>	4.3.5.1
	D	tegyem csináljam ismerjem -j-em -J <sub>MOOD</sub> -EM <sub>AGR</sub>	tedd or tegyed csináld or csináljad ismerd or ismerjed -j-ed -J <sub>MOOD</sub> -ED <sub>AGR</sub>	tegye csinálja ismerje -j-e -J <sub>MOOD</sub> -E <sub>AGR</sub>	tegyük csináljuk ismerjük -j-ük -J <sub>MOOD</sub> -UK <sub>AGR</sub>	tegyétek csináljátok ismerjétek -j-étek -J <sub>MOOD</sub> -EETEK <sub>AGR</sub>	tegyék csinálják ismerjék -j-ék -J <sub>MOOD</sub> -EEK <sub>AGR</sub>	4.3.5.2

Table S11: Hungarian verb suffixes (see text for details): Inflection by tense, mood, definiteness, and person/number. “Ind” = “Indicative”, “Cond” = “Conditional”, “Subj” = “Subjunctive”, “I” = “Indefinite”, “D” = “Definite”. For each form, we show the orthographic shape for three verbs, the suffix as identified by Rounds [2001], and our representation as a string of morphemes as described in Table S10.

FINNISH	Form	<i>juttuihisi</i>
	Lemma	<i>juttu</i>
	Annotation	Case=Ill Number=Plur Number[psor]=Sing Person[psor]=2
	Segmentation	-I-HI-SI
	Gloss	-PLURAL-ILLATIVE-2SGPOSS
HUNGARIAN	Form	<i>érveiket</i>
	Lemma	<i>érv</i>
	Annotation	Case=Acc Number=Plur Number[psor]=Plur Person[psor]=3
	Segmentation	-EK-K-ET
	Gloss	-PLURAL-POSSESSOR3RDPLUR-ACCUSATIVE
TURKISH	Form	<i>hareketlerimden</i>
	Lemma	<i>hareket</i>
	Annotation	Case=Abl Number=Plur Number[psor]=Sing Person=3 Person[psor]=1
	Segmentation	-LAR-IM-DEN
	Gloss	PLURAL-1SGPOSS-ABLATIVE

Table S12: Noun affixes in Finnish, Hungarian, and Turkish.

1. *suru*: obligatory suffix after Sino-Japanese words when they are used as verbs
2. Valence: causative (*-ase-*)
3. Voice and Mood: passive (*-are-*, *-rare-*) and potential (*-e-*, *-are-*, *-rare-*)
4. Mood: desiderative (*-ta-*)
5. Politeness (*-mas-*)
6. Polarity (Negation *-n-*)
7. Tense, Aspect, Mood: past (*-ta*), future/hortative (*-yoo*) [Kaiser et al., 2013, 229]
8. (Non-)Finiteness (*-te*)

### S1.7 Nouns in Finnish, Hungarian, and Turkish

We illustrate noun suffixes using examples taken from the corpora, with the annotation given in UD and our segmentation, in Table S12. In addition to these three slots, Hungarian also has possessed suffixes, marked with `Number[psed]` in the data. However, this is rare in the data, occurring only three times in the training set, and was thus excluded.

## S2 Other Measures of Accuracy

Here we report results using two alternative measures of accuracy. `FULLACCURACY` measures the fraction of forms (with at least two affixes) in the corpus that are ordered entirely correctly (Figure S1). `FULLTYPEACCURACY` modifies this by disregarding repeated occurrences of the same form in the corpus (Figure S2). For both measures, we only include forms that have at least two affixes; the other forms are ordered correctly under any ordering. Results across these two measures and the one reported in the main paper

strongly agree both numerically and in the qualitative patterns of the comparison between optimized orderings and baselines.

## S3 Technical Details

### S3.1 Computation of Memory-Surprisal Tradeoff

As described in the main paper, we treat word forms as sequences  $w_1 \dots w_L$  of morphemes. The basic ingredient to estimating the bound on the memory-surprisal tradeoff curve is the conditional probability of a morpheme  $w_t$  given  $t$  preceding morphemes within a word token:

$$P_t(w_k | w_{k-t} \dots w_{k-1}) \tag{1}$$

$P_t$  is defined to only depend on the relative sequence of the morphemes  $w_{k-t} \dots w_{k-1} w_k$ , not on the absolute value of  $k \in \{1, \dots, L\}$ . That is, it does not keep track of the absolute position of the morphemes in a word.

The conditional distribution  $P_t$  is defined for every  $t = 0, 1, \dots$ ; it formally defines a  $(t + 1)$ -th order Markov model. When  $w_{k-t} \dots w_{k-1}$  extends across the beginning of the word (that is, if  $k - t < 1$ ),  $P_t$  is conditioned simply on the entire prefix of length  $k - 1 < t$ . To ensure that  $P_t$  defines a proper normalized distribution over word forms (i.e., finite sequences of morphemes), we prefix and suffix morpheme sequences with special start-of-word and end-of-word symbols, respectively, in the definition of  $P_t$ .

Then, by combining Equations (6) and (7) from the main paper and plugging in the observed corpus distribution for  $P$ ,  $I_t$  (Equation 5 in the main paper) can be written as

$$I_t \equiv \mathbb{I}[w_t : w_0 | w_1 \dots w_{t-1}] \equiv \sum_{w_0 \dots w_t} \frac{F(w_0 \dots w_t)}{|C|} \log_2 \frac{P_t(w_t | w_0 \dots w_{t-1})}{P_{t-1}(w_t | w_1 \dots w_{t-1})}. \tag{2}$$

where the sum runs over all word tokens  $w_1 \dots w_L$  in the corpus and all morphemes  $w_t$  within those;  $F(w_0 \dots w_t) \in \{0, 1, 2, \dots\}$  is the frequency of the morpheme sequence  $w_0 \dots w_t$  in the corpus, and  $|C|$  is the total number of morphemes in the corpus. Evaluating Equations (6) and (7) from the main paper for every  $T = 1, 2, \dots$ , one then obtains a bound on the memory-surprisal tradeoff curve.

Following Hahn et al. [2021], we use Kneser-Ney smoothing to estimate  $P_t$ . Further following Hahn et al. [2021], disjoint sets of data are used for estimating  $P(w_t | w_0 \dots w_{t-1})$  and  $F(w_0 \dots w_t)$ : All datasets were split into *training* and *held-out* partitions. For the Universal Dependencies corpora, these were already split (we used the *validation* partitions for held-out). For Sesotho, we used the split of Hahn et al. [2021]. The heldout partition consisted of between 5% (Sesotho) and 43% (Hungarian verbs) of all tokens. We use the word form tokens in the training partition to estimate  $P_t$ , and then use the word form tokens in the held-out partition to estimate  $F$  (2). Estimating mutual information using two separate datasets in this way is a common approach with theoretical guarantees [McAllester and Stratos, 2020] that prevents an overestimation bias arising when using a single dataset.

For each language, we parameterize possible morpheme orderings through the  $N!$  possible orderings of the  $N$  affix slots. Applying any such ordering to the forms extracted from the corpus results in a set of counterfactual forms with some associated memory-surprisal tradeoff curve.

**Optimization Method** Further following Hahn et al. [2021], we optimize orderings using an adaptation of the hill-climbing method originally devised by Gildea and Temperley [2007] for optimizing word order. The algorithm randomly initializes the ordering of slots. It then iteratively changes it to decrease AUC. In every

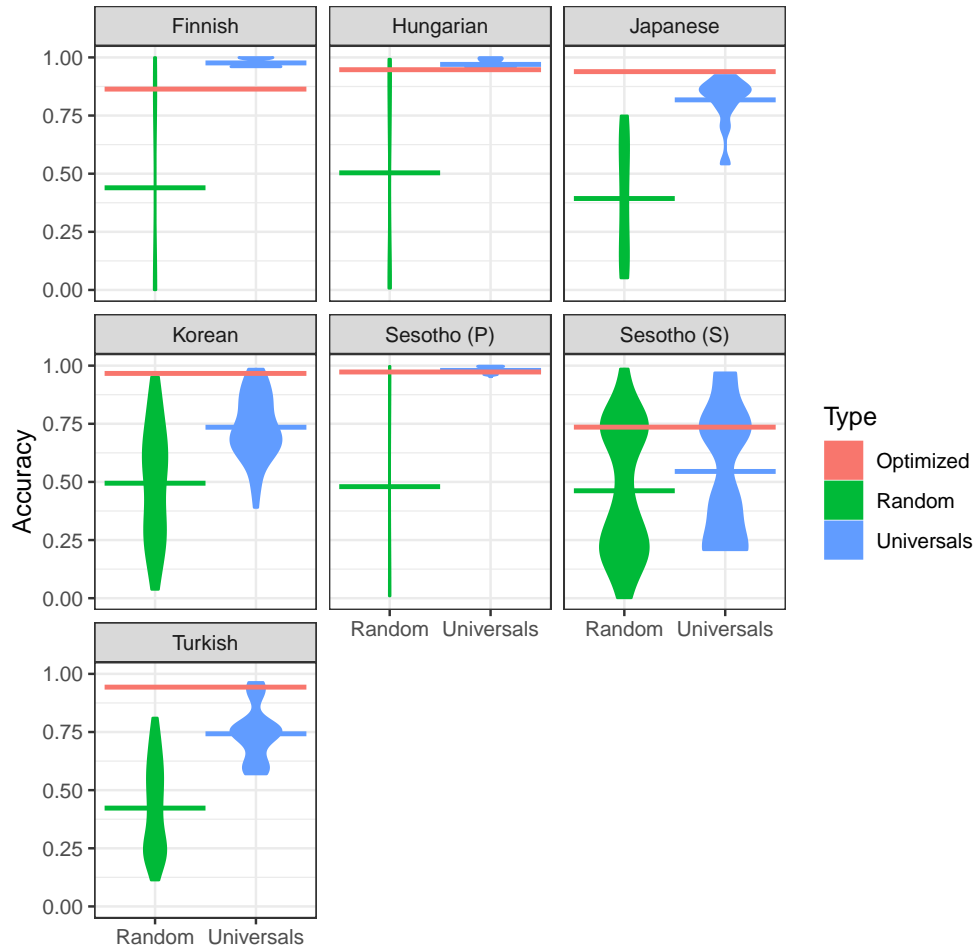


Figure S1: Accuracies in predicting verb morpheme ordering, according to the FULLACCURACY measure. For the baselines, we provide both a smoothed violin plot of the distribution of accuracies, and the mean accuracy as a horizontal line (green and blue). For the optimized order, we show the accuracy as a horizontal line (red). In all languages, optimized orderings provide higher accuracy than the mean of the random baselines at  $p < 0.001$ .

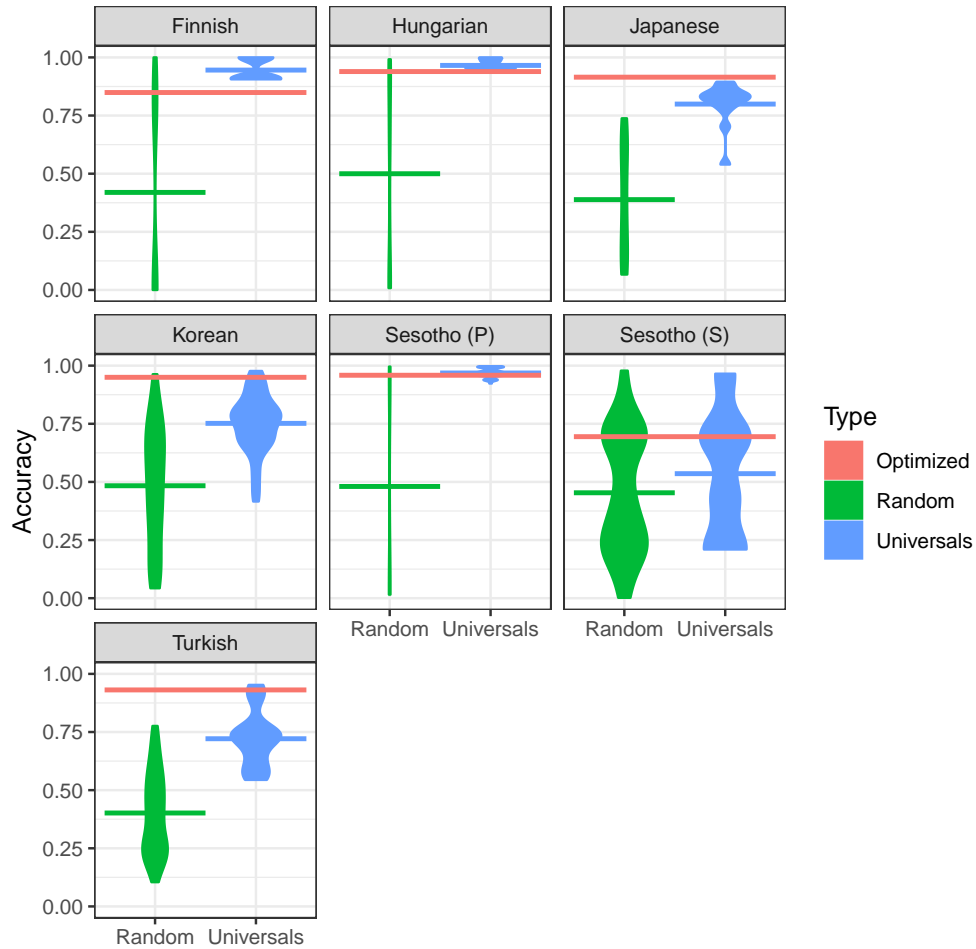


Figure S2: Accuracies in predicting verb morpheme ordering, according to the FULLTYPEACCURACY measure. For the baselines, we provide both a smoothed violin plot of the distribution of accuracies, and the mean accuracy as a horizontal line (green and blue). For the optimized order, we show the accuracy as a horizontal line (red). In all languages, optimized orderings provide higher accuracy than the mean of the random baselines at  $p < 0.001$ .

iteration, it randomly chooses a slot, and moves it to some other position (between two other slots, or at the beginning or end) in such a way to maximally decrease AUC. To speed up computation, slots occurring fewer than 10 times are sampled only in about 5% of iterations, and the algorithm considers only a random subset of about half of all possible positions in every iteration. Optimization runs for 1,000 iterations, empirically sufficient to guarantee convergence. Due to the difficulty of combinatorial optimization, this algorithm is not guaranteed to find the global optimum. However, as Gildea and Temperley [2007] previously, we find its results to be consistent across runs and to have lower AUC than all randomly sampled orderings.

**On the Role of Conditional Mutual Information** We note that some prior work has considered the role of unconditional mutual information  $I[w_t : w_0]$  in human language [e.g. Ebeling and Pöschel, 1994, Futrell et al., 2020], whereas the bounds used here are based on conditional mutual information. Informally, the choice of conditional mutual information reflects the fact that utilizing information from the distant past induces memory load only to the extent that it is not redundantly reflected in the intervening material; conditional mutual information only reflects those bits of predictive information that cannot be redundantly inferred from intervening material. Corresponding theoretical bounds on memory load cannot be obtained in general considering only unconditional mutual information [Hahn et al., 2021].

### S3.2 Example Computation of Memory-Surprisal Tradeoff

Here, we provide an example for the calculation of the bound on the memory-surprisal tradeoff curve and its AUC, using the example of Sesotho verb suffixes, comparing real and reverse orderings.

**Conditional Mutual Information** Recall that the conditional mutual information  $I_t$  is defined as (Equation 2):

$$I_t \equiv I[w_t : w_0 | w_1 \dots w_{t-1}] \equiv \sum_{w_0 \dots w_t} \frac{F(w_0 \dots w_t)}{|C|} \log_2 \frac{P_t(w_t | w_0 \dots w_{t-1})}{P_{t-1}(w_t | w_1 \dots w_{t-1})}. \quad (3)$$

The resulting curve for Sesotho suffixes is shown in Figure S3 (bottom left). There is a difference, though barely perceptible, whereby  $I_t$  decays faster for the real orderings than for the reverse orderings.

To understand whether this difference is meaningful, it is helpful to consider  $I_t$  for individual suffix classes. In Figure S3 (top), we show this quantity separately for the different types of suffixes in Sesotho, that is, we restrict the summation  $\sum_{w_0 \dots w_t}$  and the normalization constant  $|C|$  to those sequences where  $w_t$  is an affix of a specific morphological category. The results show that, for several of the affix classes, the decay of  $I_t$  is distinctively steeper for the real ordering than the reverse ordering. For instance, for the Derivation affix class, conditional mutual information with the immediately preceding morpheme is substantially higher in the real orderings (where the preceding morpheme is the root) than in reverse orderings (where the preceding morpheme is an inflectional morpheme). As described in the main paper, such a steep fall-off indicates that predictive information is concentrated in the recent past, which reduces the memory load needed for accurate prediction. Importantly, no affix class shows a clear pattern in the reverse direction.

By averaging these curves, weighted by the corpus frequency of different affix types, one obtains the overall curves for  $I_t$  shown in Figure S3 (bottom left). The resulting curves mirror the pattern observed in the individual curves, though the numerical difference between real and reverse orderings is small: This is a common phenomenon when calculating memory-surprisal tradeoffs: It turns out that the Mood affix is by far the most common one, and thus dominates the overall average information. In general, high-frequency morphemes will tend to be less sensitive to ordering differences, because their high frequency makes them



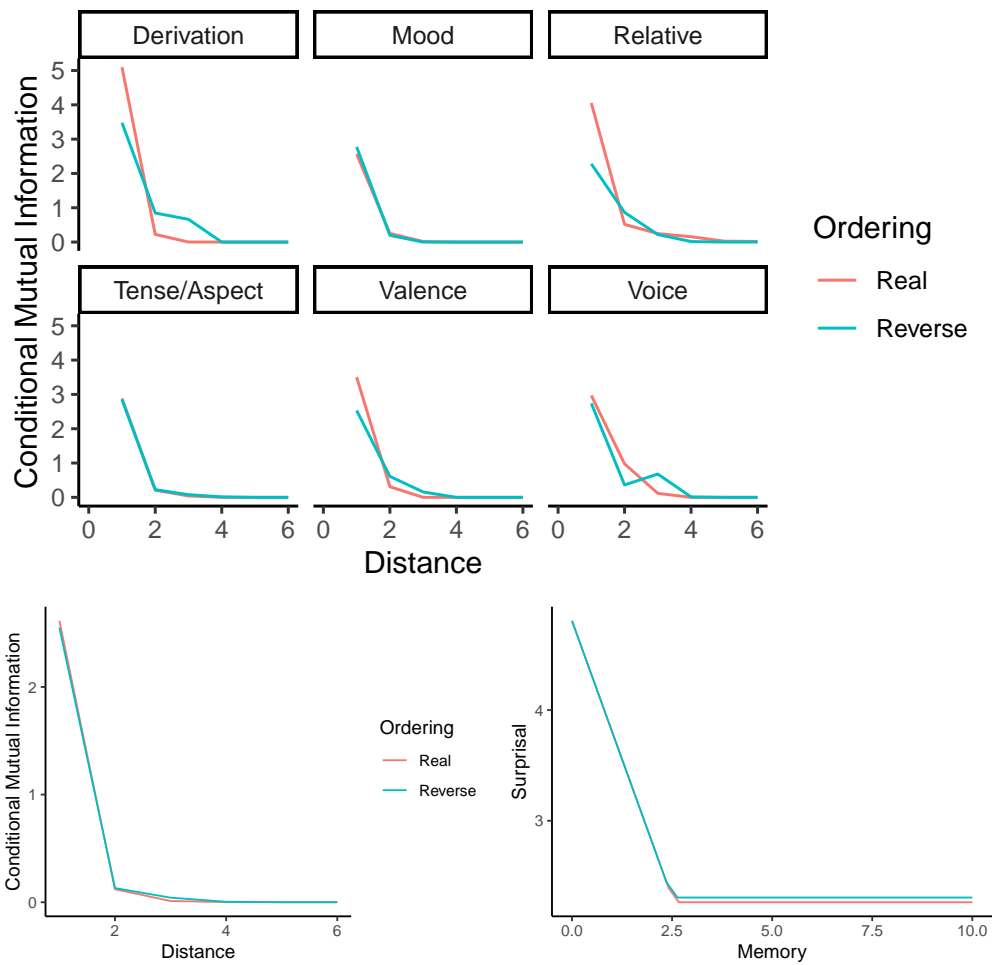


Figure S3: Conditional mutual information  $I_t$  (top and bottom left) and memory-surprisal tradeoff (bottom right) for Sesotho verb suffixes. See text for details.

always relatively easy to predict. Differences between the efficiency of different orderings are thus typically driven by lower-frequency affixes for which ordering strongly impacts how easy they are to predict from their immediate context. Considering affix classes individually shows that the overall difference, even though small, is meaningful.

**Tradeoff Curve** By further applying Equations (6–7) from the main paper and tracing out all values of  $T = 1, 2, 3, \dots$ , one then obtains a bound on the memory-surprisal tradeoff curves, shown in Figure S3 (bottom right). More specifically, for every  $T = 1, 2, 3, \dots$ , one computes memory capacity as

$$M_T := \sum_{t=1}^T tI_t. \quad (4)$$

and surprisal as

$$S_T := S_\infty + \sum_{t=T+1}^{\infty} I_t. \quad (5)$$

By connecting these points, one obtains a bound on the tradeoff curve as shown in Figure S3 (bottom right). Due to the factor  $t$  inside  $M_T$ , a steeper fall-off in  $I_t$  translates into lower memory capacity  $M_T$  needed for the same level of surprisal  $S_T$ . For some sufficiently large  $T_{max}$  (bounded by the length of the longest word form in the corpus),  $I_{T_{max}}$  will become zero, and  $M_T$  and  $S_T$  will not change any more as  $T$  increases beyond  $T_{max}$ . In this case,  $S_{T_{max}}$  will equal  $S_\infty$ , the surprisal obtained with perfect memory. In the case of Figure S3 (bottom left), this situation is attained at  $T_{max} = 4$ . For any comprehender with memory capacity greater than  $M_{T_{max}}$ , surprisal will still be at least  $S_{T_{max}} = S_\infty$ ; thus, the tradeoff curve in theory extends infinitely to the right horizontally (we show it up to  $M = 10$  in the figure).

These curves reflect the Pareto frontiers for possible comprehenders: For any comprehender, its average surprisal and average memory usage cannot lie below the curve. The real orderings have a slightly more efficient tradeoff than the reverse orderings, as surprisal is lower at high memory capacities. Again, the numerical difference between real and reverse orderings appears small, but we note that this difference applies, on average, at every single morpheme in every word. A small change in the per-morpheme surprisal can lead to more significant change in overall surprisal across a word form or a sentence. Specifically, while the average difference is small, considering  $I_t$  separately for affix classes (Figure S3, top) shows that substantial surprisal differences should be expected on derivational affixes, relative clause markers, and valence and voice affixes.

**AUC** The AUC measure used for determining the overall efficiency of an ordering is then derived by calculating the area under the tradeoff curve; this is smaller when the tradeoff curve decays faster. As the tradeoff curve in theory extends infinitely to the right, AUC needs to be restricted to some arbitrary upper bound  $M_{max}$  on memory, for which we follow Hahn et al. [2021] in taking  $M_{max} = 10$  as in Figure S3 (bottom right) across all languages. Note that, while the choice of  $M_{max}$  substantially impacts the *absolute value* of AUC, impact on the *relative efficiencies* of different orderings is negligible. Geometrically, a smaller AUC indicates that the set below the Pareto frontier, the set of “impossible comprehenders”, is smaller, indicating a more efficient tradeoff.

**Efficiency and  $S_\infty$**  In the specific case of Figure S3, not only the tradeoff’s efficiency, but also the overall surprisal  $S_\infty$  differs between the two orderings even at unbounded memory, though this does not always have to be the case [see Hahn et al., 2021, for more discussion]. Figure S3 shows that, for several suffix types, the

real and reverse orderings contain similar amounts of overall predictive information about the affix, but the real ordering places it at a smaller distance, which creates a more efficient tradeoff.

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